# 2. QCD & SM examples

- I. QCD corrections
- II. Jets
- III. Hunting the Higgs at the LHC
- IV. Top quark mass measurement

 In order to have precise predictions working at LO might not be enough



[Stirling-Pascos 2011]



• In order to have precise predictions working at LO might not be enough



[Stirling-Pascos 2011]

## I. QCD corrections

Total Cross Section



Can we use pQCD despite confinement? "YES"



\* The  $\gamma/Z$  virtuality is  $Q = \sqrt{s}$ \* Production occurs at a distance  $\simeq \frac{1}{Q}$ \* Q is large  $\implies$  pQCD applicable

- Hadronization changes quarks and gluons to hadrons.
- $\checkmark$  Hadronization takes place at a scale  $\frac{1}{\Lambda}$ .
- The change in the outgoing state occurs too late to modify the probability of the event to happen!
- Details of the final state certainly are changed.

### Lowest Order Result ( $\alpha_s^0$ )

 $\checkmark$  For simplicity, we neglect the Z contribution (i.e.  $\sqrt{s} \ll M_Z$ )

$$\frac{d\sigma_0}{d\cos\theta} = \frac{\pi\alpha^2 Q_f^2}{2s} N_c \left(1 + \cos^2\theta\right) \implies \sigma_0 = \frac{4\pi\alpha^2}{3s} N_c Q_f^2$$

leading to

$$R_0 \equiv \frac{\sigma(e^+e^- \to \text{hadrons})}{\sigma(e^+e^- \to \mu^+\mu^-)} = N_c \sum_q Q_q^2$$

 $\rightleftharpoons$  At the Z pole (i.e. neglecting  $\gamma$ ), we have

$$R_{0} = N_{c} \frac{\sum_{q} \left(A_{q}^{2} + V_{q}^{2}\right)}{A_{\mu}^{2} + V_{\mu}^{2}}$$





After adding all contributions the UV divergences cancel out (Ward identity). The same happens for the IR ones!

$$R = R_0 \left( 1 + \frac{\alpha_s(\mu)}{\pi} \right) \longrightarrow R_0 \left( 1 + \frac{\alpha_s(\sqrt{s})}{\pi} \right)$$

Unlike UV divergences, there is no renormalization for the IR ones. They indicate sensitivity to long range physics like masses, hadronization process, etc.

→ The singularities are not physical; they indicate the breakdown of the perturbative approach. Quarks and gluons are never on mass-shell-particles and we can not ignore the effects of confinement at a scale  $\simeq 1$  GeV.

General form of the IR divergences for  $p_q \rightarrow 0$ 

$$\sigma^{q\overline{q}g} = \frac{2\alpha_s}{3\pi}\sigma_{q\overline{q}}\int d\cos\theta_{qg}\frac{dE_g}{E_g}\frac{4}{(1-\cos\theta_{qg})(1+\cos\theta_{qg})}$$

# NLO in hadron colliders

The parton model expression for cross sections is

 $egin{aligned} \sigma &= \sum_{ij} rac{1}{1+\delta_{ij}} \int dx_1 \ dx_2 & \left\{ f_i(x_1,Q_F^2) f_j(x_2,Q_F^2) \ + \ i \leftrightarrow j 
ight\} \otimes \ & \hat{\sigma}_{ij}(lpha_s(Q_R^2),Q_R^2,Q_F^2;x_1x_2s) \end{aligned}$ 

 $\checkmark$  Expanding the pdf's and  $\hat{\sigma}$  ( $X = X^{(0)} + X^{(1)} + \cdots$ ) the lowest order term is

$$\sigma = \sum_{ij} \frac{1}{1+\delta_{ij}} \int dx_1 \, dx_2 \left\{ f_i^{(0)}(x_1) f_j^{(0)}(x_2) + i \leftrightarrow j \right\} \otimes \hat{\sigma}_{ij}^{(0)}(x_1 x_2 s)$$

The NLO contribution is obtained through

 $[f_i^{(1)}f_j^{(0)} + f_i^{(0)}f_j^{(1)} + i \leftrightarrow j] \times \hat{\sigma}^{(0)} \oplus [f_i^{(0)}f_j^{(0)} + i \leftrightarrow j] \times \hat{\sigma}^{(1)}$ 

The red term contains collinear divergences that are canceled by the divergences in the blue term.

## • Scales:

• The evaluation of  $\hat{\sigma}$  contains a UV divergence => renormalization => remnant of the process is the renormalization scale  $\mu_R$ 

- Full calculation should not depend on  $\mu_R$  => we can estimate the higher order corrections by the  $\mu_R$  dependence
- At each order, the subprocess cross section and the PDF's have a residual factorization scale dependence on  $\mu_F$
- The residual scale dependence should improve with higher order calculations

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(C. Anastasiou, L. Dixon, K. Melnikov, F. Petriello, PRL 91 (2003) 182002)



# II. Jets

 $\Leftrightarrow$  Can we obtain more information on the hadron production besides the total cross section?

 $\checkmark$  We expect that soft process don't change completely the high energy features  $\implies$  a spray of hadrons follows the direction of the original quarks and gluons.



#### Three jet event:

why not 4?
Which particles belong to a jet?
how to get

$$p_{parton} \simeq p_{jet}$$
 ?



#### Not an easy task:



- I. Simple to implement in an experimental analysis
- 2. Simple to implement in a theoretical calculation
- 3. Defined at any order of perturbation theory
- 4. Yields finite cross sections at any order of PT
- 5. Yields a cross section rather insensitive to hadronization

## A few jet algorithms

- Three popular jet algorithms are kT, anti-kT, and Cambridge/Aachen
- The distance and rule to join objets is

$$\mathbf{d_{ij}} = \min[\mathbf{p_{Ti}^{2\alpha}}, \mathbf{p_{Ti}^{2\alpha}}] \ \left(\frac{\Delta \mathbf{R_{ij}}}{\mathbf{R}}\right)^2 \quad \text{and} \quad \mathbf{d_{iB}} = \mathbf{p_{Ti}^{2\alpha}}$$

with  $\Delta R_{ij} = \sqrt{\Delta \eta_{ij}^2 + \Delta \varphi_{ij}^2}$ 

repeatedly combine objets until  ${\rm d}_{i{\rm B}}$  is the smaller distance. Then call it a jet, remove from the list and start again

•The choices are: kT ( $\alpha = 1$ ); anti-kT ( $\alpha = -1$ ); C/A ( $\alpha = 0$ )


















































This expression also describes well the y dependence





• The basic expression for 2 to 2 processes is

$$\frac{d\sigma}{dp_T^2} = \sum_{ij} \int dx_1 dx_2 \, \frac{f_i(x_1, Q_F^2) f_j(x_2, Q_F^2)}{(1 + \delta_{ij})} \, \times \, \frac{d\hat{\sigma}}{dp_T^2}$$

+ In the jet-jet CMS  $\implies dy_1 dy_2 dp_T^2 = \frac{1}{2} s dx_1 dx_2 d \cos \theta^*$ 

$$rac{d^3\sigma}{dy_1dy_2dp_T^2} = rac{1}{16\pi s^2} \sum_{ij} rac{f_i(x_1,Q_F^2)f_j(x_2,Q_F^2)}{(1+\delta_{ij})x_1x_2} imes \overline{\sum} |M(ij o kl)|^2$$
 with

$$x_1 = rac{x_T}{2} \left( e^{y_1} + e^{y_2} 
ight) ; \quad x_2 = rac{x_T}{2} \left( e^{-y_1} + e^{-y_2} 
ight) \quad \mathbf{x_T} = rac{2\mathbf{p_T}}{\sqrt{\mathbf{s}}}$$

Process	$rac{32\pi^2}{lpha_s^2} \; rac{d\hat{\sigma}}{d\Omega}$	at 90 degrees
$qq' \rightarrow qq'$	$rac{1}{2\hat{s}}rac{4}{9}rac{\hat{s}^2+\hat{u}^2}{\hat{t}^2}$	2.2
$qq \rightarrow qq$	$\frac{1}{2} \frac{1}{2\hat{s}} \left[ \frac{4}{9} \left( \frac{\hat{s}^2 + \hat{u}^2}{\hat{t}^2} + \frac{\hat{s}^2 + \hat{t}^2}{\hat{u}^2} \right) - \frac{8}{27} \frac{\hat{s}^2}{\hat{u}\hat{t}} \right]$	3.3
$q \bar{q} \rightarrow q' \bar{q}'$	$rac{1}{2\hat{s}}rac{4}{9}rac{\hat{t}^2+\hat{u}^2}{\hat{s}^2}$	0.2
$q\bar{q} \rightarrow q\bar{q}$	$\frac{1}{2\hat{s}} \left[ \frac{4}{9} \left( \frac{\hat{s}^2 + \hat{u}^2}{\hat{t}^2} + \frac{\hat{t}^2 + \hat{u}^2}{\hat{s}^2} \right) - \frac{8}{27} \frac{\hat{u}^2}{\hat{s}\hat{t}} \right]$	2.6
$q \bar{q}  ightarrow gg$	$rac{1}{2}rac{1}{2\hat{s}}\left[rac{32}{27}rac{\hat{t}^2+\hat{u}^2}{\hat{t}\hat{u}}-rac{8}{3}rac{\hat{t}^2+\hat{u}^2}{\hat{s}^2} ight]$	1.0
$gg \rightarrow q\bar{q}$	$rac{1}{2\hat{s}}\left[rac{1}{6}rac{\hat{t}^2+\hat{u}^2}{\hat{t}\hat{u}}-rac{3}{8}rac{\hat{t}^2+\hat{u}^2}{\hat{s}^2} ight]$	0.1
$  gq \rightarrow gq$	$rac{1}{2\hat{s}}\left[-rac{4}{9}rac{\hat{s}^2+\hat{u}^2}{\hat{s}\hat{u}}+rac{\hat{u}^2+\hat{s}^2}{\hat{t}^2} ight]$	6.1
gg  ightarrow gg	$rac{1}{2}rac{1}{2\hat{s}}rac{9}{2}\left(3-rac{\hat{t}\hat{u}}{\hat{s}^2}-rac{\hat{s}\hat{u}}{\hat{t}^2}-rac{\hat{s}\hat{t}}{\hat{u}^2} ight)$	30.4

+ The LO processes leading to jets are (gluon in the *t*-channel)

with  $\hat{t} = -\hat{s} \; (1 - \cos \theta)/2$  and  $\hat{u} = -\hat{s} \; (1 + \cos \theta)/2$ 

#### Tevatron results

# the inclusive jet cross section does agree with NLO QCD over 8 orders of magnitude!



•Let's look the results without the dirt trick of log plots





the inclusive jet cross section is nicely described by NLO QCD



#### a more serious comparison



# V. Hunting the SM Higgs



# V. Hunting the SM Higgs

Higgs production mechanisms and cross sections



• We must take into account the H decays



 $H \to W^+ W^- \to \ell^+ \ell^- E_T + 0, 1, 2 \text{ jets}$ 

Cuts used in the analyses

$m_{ m H}$	$p_{\mathrm{T}}^{\ell,\mathrm{max}}$	$p_{\mathrm{T}}^{\ell,\mathrm{min}}$	$m_{\ell\ell}$	$\Delta \phi_{\ell\ell}$	$m_T^{\ell\ell E_{\mathrm{T}}^{\mathrm{miss}}}$
$[\text{GeV}/c^2]$	[GeV/c]	[GeV/c]	$[\text{GeV}/c^2]$	[dg.]	$[GeV/c^2]$
	>	>	<	<	[,]
120	20	10(15)	40	115	[80,120]
130	25	10(15)	45	90	[80,125]
160	30	25	50	60	[90,160]
200	40	25	90	100	[120,200]
250	55	25	150	140	[120,250]
300	70	25	200	175	[120,300]
400	90	25	300	175	[120,400]



 $H \to W^+ W^- \to \ell^+ \ell^- E_T + 0, 1, 2 \text{ jets}$ 

Cuts used in the analyses

$m_{ m H}$	$p_{\mathrm{T}}^{\ell,\mathrm{max}}$	$p_{\mathrm{T}}^{\ell,\mathrm{min}}$	$m_{\ell\ell}$	$\Delta \phi_{\ell\ell}$	$m_T^{\ell\ell E_{\mathrm{T}}^{\mathrm{miss}}}$
$[\text{GeV}/c^2]$	[GeV/c]	[GeV/c]	$[\text{GeV}/c^2]$	[dg.]	$[GeV/c^2]$
	>	>	<	<	[,]
120	20	10(15)	40	115	[80,120]
130	25	10(15)	45	90	[80,125]
160	30	25	50	60	[90,160]
200	40	25	90	100	[120,200]
250	55	25	150	140	[120,250]
300	70	25	200	175	[120,300]
400	90	25	300	175	[120,400]



Δφ<sub>..</sub> [°]

 $H \to W^+ W^- \to \ell^+ \ell^- E_T + 0, 1, 2 \text{ jets}$ 

Cuts used in the analyses

$m_{ m H}$	$p_{\mathrm{T}}^{\ell,\mathrm{max}}$	$p_{\mathrm{T}}^{\ell,\mathrm{min}}$	$m_{\ell\ell}$	$\Delta \phi_{\ell\ell}$	$m_T^{\ell\ell E_{\mathrm{T}}^{\mathrm{miss}}}$
$[\text{GeV}/c^2]$	[GeV/c]	[GeV/c]	$[\text{GeV}/c^2]$	[dg.]	$[GeV/c^2]$
	>	>	<	<	[,]
120	20	10(15)	40	115	[80,120]
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160	30	25	50	60	[90,160]
200	40	25	90	100	[120,200]
250	55	25	150	140	[120,250]
300	70	25	200	175	[120,300]
400	90	25	300	175	[120,400]



Data describes predicted background well.



- Low branching ratio but great mass resolution (similar to 4 leptons)
- Useful in the range  $110 < M_H < 150 \text{ GeV}$
- requirement: two energetic photons
- signal is an excess over a "smooth" falling background
- Main backgrounds:  $pp \to \gamma\gamma$  ;  $pp \to \gamma$  jet ;  $pp \to j$ et + jet
- Tight photon requirements



# **Observed** limits



### **Observed** limits



## Combining all search channels



# Combining all channels



Light Higgs production via WBF (good for 14 TeV)

 $\pmb{\ast}$  We can tag the final state jets in  $\mathbf{q}\mathbf{q} \to \mathbf{H}\mathbf{q}\mathbf{q} \to \mathbf{H}\mathbf{j}\mathbf{j}$ 

\* Let's focus on  $\mathbf{H} \to \tau^+ \tau^- \to \mathbf{e}^\mp \mu^\pm p_T$ 

\* The main backgrounds are (write the subprocesses)

- $t\overline{t} + n$  jets with n = 0, 1, 2. The extra jet is a tagging jet.
- $\mathbf{b}\mathbf{\bar{b}jj}$  with  $\mathbf{b} \rightarrow \nu \ell \mathbf{c}$
- QCD  $\tau \tau j j$  that are higher order of DY  $\mathbf{Z} \rightarrow \tau \tau$
- EW ττjj: WBF of Z's
- QCD and EW WWjj production

#### \* The main cuts are:

Rapidity gap and acceptance cuts

$$\begin{split} p_{T_j} &\geq 20 \; \text{GeV} \;, \; \; |\eta_j| \leq 5.0 \;, \; \; \bigtriangleup R_{jj} \geq 0.7 \\ p_{T_\ell} &\geq 10 \; \text{GeV} \;, \; \; |\eta_\ell| \leq 2.5 \;, \; \; \bigtriangleup R_{j\ell} \geq 0.7 \\ &\bigtriangleup R_{e\mu} \geq 0.4 \;, \\ \eta_{j,min} + 0.7 < \eta_{\ell_{1,2}} < \eta_{j,max} - 0.7 \;, \\ &\eta_{j_1} \cdot \eta_{j_2} < 0 \\ &\bigtriangleup \eta_{tags} = |\eta_{j_1} - \eta_{j_2}| \geq 4.4 \;, \end{split}$$

,

- b-veto:  $p_{T_b} > 20 \text{ GeV}$ ,  $\eta_{j,\min} < \eta_b < \eta_{j,\max}$ .
- Missing transverse momentum  $p_T > 30 \text{ GeV}$

Arbitrary units Higgs signal mu=160 GeV/c<sup>2</sup> tt background a) 0.02 0.01 0 -2 0 2 η  $1/\sigma d\sigma/dp_{T} (GeV^{-1})$ 25 50 75 100 125 150 0

 $p_{T}$  (GeV)

•  $M_{jj} > 800 \text{ GeV}$ 

•  $\tau \tau$  reconstruction:  $\mathbf{M}_{\tau \tau} = \mathbf{m}_{e\mu} / \sqrt{\mathbf{x}_{\tau_1} \mathbf{x}_{\tau_2}}$ 

$$\begin{split} &\cos \phi_{e\mu} \ > \ -0.9 \ . \\ &x_{\tau_1}, \ x_{\tau_2} > 0 \ , \\ &x_{\tau_1}^2 + x_{\tau_2}^2 < 1 \ . \end{split}$$

- Lepton correlations:  $\triangle R_{e\mu} < 2.6$
- minijet veto:

$$\mathbf{p_{Tj}^{veto}} > \mathbf{p_{T,veto}}$$
;  $\eta_{j,min}^{tag} < \eta_{j}^{veto} < \eta_{j,max}^{tag}$ 



#### **\*** Effect of the cuts for $M_{\rm H} = 120$ GeV and a bins $\pm 10$ GeV

	$H \to \tau \tau$	QCD	EW			QCD	EW	
cuts	signal	au au j j	au au j j	$tar{t}+jets$	$b\overline{b}jj$	WWjj	WWjj	S/B
forward tags	1.34	4.7	0.18	45	8.2	0.18	0.11	1/44
+ b veto				2.6				1/12
$+ p_T$	1.17	2.3	0.12	2.0	0.28	0.12	0.08	1/4.1
$+ M_{ii}$	0.92	0.67	0.10	0.53	0.13	0.049	0.073	1/1.7
+ non- $\tau$ reject.	0.87	0.58	0.10	0.09	0.10	0.009	0.012	1/1
+ $\Delta R_{e\mu}$	0.84	0.52	0.086	0.087	0.028	0.009	0.011	1.1/1
+ ID effic. ( $\times 0.67$ )	0.56	0.34	0.058	0.058	0.019	0.006	0.008	1.1/1
$P_{surv,20}$	$\times 0.89$	$\times 0.29$	$\times 0.75$	$\times 0.29$	$\times 0.29$	imes 0.29	$\times 0.75$	-
+ minijet veto	0.50	0.100	0.043	0.017	0.006	0.002	0.006	2.7/1

#### **\*** Contamination from $\mathbf{H} \to \mathbf{W}\mathbf{W}$

$M_{H}$	115	120	125	130	135	140	145	150
$B(H \to \tau \tau) \cdot \sigma$ (fb)	0.93	0.84	0.74	0.62	0.51	0.39	0.27	0.19
$B(H  o WW) \cdot \sigma$ (fb)	0.015	0.024	0.034	0.045	0.057	0.067	0.072	0.076

#### Even after full simulation the Higgs signal is nice

#### $* \tau \tau$ channel



#### WW channel



### IV.Top mass measurement

Top mass measurement in  $t\bar{t} \rightarrow jjb (e/\mu)\nu b$  at 14 TeV

Main background and their size

Process	$\sigma$ (pb)
signal	250
$\mathbf{bb} \rightarrow \ell \nu + jets$	$\mathbf{2.2  imes 10^6}$
$\mathbf{W} + jets \rightarrow \ell \nu + jets$	$7.8 imes10^3$
$\mathbf{Z} + \text{ jets} \rightarrow \ell^+ \ell^- + \text{ jets}$	$7.8 imes10^3$
$\mathbf{WW} \rightarrow \ell \nu + jets$	17.1
$\mathbf{WZ}  ightarrow \ell  u + jets$	3.4
$\mathbf{ZZ} \rightarrow \ell^+ \ell^- + \text{ jets}$	<b>9.2</b>

 $\mathbf{S}/\mathbf{B} \simeq 10^{-4}$  This is not as bad as it looks.

#### Event selection

- 1 isolated  $e^{\pm}$  or  $\mu^{\pm}$  with  $p_{T} > 20$  GeV and  $|\eta| < 2.5$
- $\mathbb{E}_T > \mathbf{20} \text{ GeV}$  .
- 2 tagged b quarks with  $\mathbf{p}_{\mathrm{T}} > 40$  GeV and  $|\eta| < 2.5$
- 2 light jets with  $\mathbf{p_T} > \mathbf{40} \; \mathsf{GeV}$  and  $|\eta| < \mathbf{2.5}$

	Process	Cross-section (pb)	Total efficiency (%)
Atter Cuts	$tar{t}$ signal	250	3.5
${f S}/{f B}\simeq 78$	$b \overline{b}  ightarrow l  u + jets$	$2.2  imes 10^6$	$3 \times 10^{-8}$
87k events	W+jets  ightarrow l u+jets	$7.8  imes 10^3$	$2  imes 10^{-4}$
for 10 fb $-1$	$Z+jets  ightarrow l^+l^-+jets$	$1.2  imes 10^3$	$6 imes 10^{-5}$
	WW  ightarrow l u + jets	17.1	$7 imes 10^{-3}$
	WZ  ightarrow l u + jets	3.4	$1 \times 10^{-2}$
	$ZZ  ightarrow l^+l^- + jets$	9.2	$3 \times 10^{-3}$
**\*** Top quark mass from  $\mathbf{t} \to \mathbf{bjj}$ 

- The event present ≥ 4 jets (ISR and FSR)
- Recontruct the W:  $|\mathbf{M}_{jj} - \mathbf{M}_{\mathbf{W}}^{\mathbf{PDG}}| < 20 \text{ GeV}$ (purity 66%)
- choose the b-tagged jet leading to highest  $\mathbf{p}_{\mathrm{T}}^{\mathrm{top}}$  (81%)



\* Possible to measure  $M_t$  with a precision  $\simeq 1.3$  GeV (systematic) for 10 fb<sup>-1</sup>



## backup: top mass

• The different algorithms lead to distinct jets shapes when they overlap

kT (I) starts around softer objects



C/A (0) cares only about distances



anti-kt (-1) clusters around hard objects



 $\mathbf{d_{ij}} = \min[\mathbf{p_{Ti}^{2\alpha}}, \mathbf{p_{Ti}^{2\alpha}}] \ \left(\frac{\Delta R_{ij}}{R}\right)^2 \quad \text{and} \quad \mathbf{d_{iB}} = \mathbf{p_{Ti}^{2\alpha}}$ 

 $p_T^A > p_T^B$ 

## [JHEP04 (2008) 063]









## IV. Anomalous couplings

conservation

Triple gauge-boson vertices

(hep-ph/0506074)

30

SM gauge fixes TGV We have already observed  $W^+W^-\gamma$  and  $W^+W^-Z$ Hypothesis: *C* and *P* 

20-10-VFSWW/RacoonWW no 2WW vertex (Gentle) 0-160 180 200

√s (GeV)

LEP

PRELIMINARY

☆ Deviations from SM in terms of 5 new parameters

$$\mathcal{L}_{\text{eff}}^{\text{WWV}} = -ig_{\text{WWV}} \left[ g_{1}^{V} (W_{\mu\nu}^{+} W^{-\mu} - W_{\mu\nu}^{-} W^{+\mu}) V^{\nu} + \kappa_{V} W_{\mu}^{+} W_{\nu}^{-} V^{\mu\nu} + \frac{\lambda_{V}}{M_{W}^{2}} W_{\mu}^{+\nu} W_{\nu}^{-\rho} V_{\rho}^{\mu} \right]$$

 $rac{1}{2}$  smoking gun:  $\hat{\sigma}$  grows with  $\sqrt{\hat{s}}$ 

 We must introduce form factors  $(1+Q^2/\Lambda^2)^{-n}$ 

NLO available; uncertainties PDFs

 $rightarrow \mathbf{pp} 
ightarrow \mathbf{W} \gamma (\mathbf{Z})$ : limits fitting  $\mathbf{p_T^V}$ 





## 🖈 Attainable 95% CL limits

anomalous coupling	direct LEP limits	indirect limits	pair production limits at the LHC
$\Delta \kappa_{\gamma}$	[-0.105, 0.069]	$[-0.044 \ , \ 0.059]$	$[-0.034 \ , \ 0.034]$
$\lambda_{\gamma}$	[-0.059, 0.026]	[-0.061 , 0.10]	[-0.0014, 0.0014]
$g_1^Z$	[-0.051, 0.034]	[-0.051, 0.0092]	[-0.0038, 0.0038]
$\Delta \kappa_Z$	[-0.040, 0.046]	[-0.050 , 0.0039]	[-0.040 , 0.040]
$\lambda_Z$	[-0.059, 0.026]	[-0.061, 0.10]	[-0.0028, 0.0028]

The statistics will be enough to measure the form factors:



- Presently not enough data have been analyzed at LHC
- ATLAS analyzed 1 fb<sup>-1</sup> of  $WZ \to \ell \ell \ell E_T$  (71 events)
- - Main backgrounds: ZZ, W/Z+ jets,  $t\bar{t}$ ,  $W/Z + \gamma$

Final State	$eee + E_{\rm T}^{\rm miss}$	$ee\mu + E_{\mathrm{T}}^{\mathrm{miss}}$	$e\mu\mu+E_{ m T}^{ m miss}$	$\mu\mu\mu + E_{ m T}^{ m miss}$	Combined
Observed	11	9	22	29	71
ZZ	$0.4{\pm}0.0$	$1.0 \pm 0.1$	$0.8 {\pm} 0.1$	$1.7 \pm 0.1$	$3.9{\pm}0.1{\pm}0.2$
W/Z+jets	$2.0 \pm 0.5$	$0.7 \pm 0.3$	$1.7 \pm 0.5$	$0.4 \pm 0.3$	$4.8 \pm 0.8^{+4.0}_{-1.9}$
Top	$0.2 \pm 0.1$	$0.8 \pm 0.6$	$0.9 \pm 0.7$	$0.4 \pm 0.5$	$2.3 \pm 1.0 \pm 0.5$
$W/Z + \gamma$	$0.5 {\pm} 0.3$	_	$0.6 {\pm} 0.4$	_	$1.1{\pm}0.5{\pm}0.1$
Total Background	$3.1 {\pm} 0.6$	$2.5 {\pm} 0.7$	$3.9{\pm}0.9$	$2.6 {\pm} 0.6$	$12.1 \pm 1.4^{+4.1}_{-2.0}$
Expected Signal	$7.7 \pm 0.2$	$11.6 \pm 0.2$	$12.4 \pm 0.2$	$18.6 {\pm} 0.3$	$50.3 {\pm} 0.4 {\pm} 4.3$



• little statistics to do a fit => use total cross section

Coupling	Observed	Observed	Expected
	$(\Lambda = 2 \text{ TeV})$	$(\Lambda = \infty)$	$(\Lambda = \infty)$
$\Delta g_1^Z$	[-0.20, 0.30]	[-0.16, 0.24]	[-0.12, 0.20]
$\Delta \kappa_Z$	[-0.9, 1.1]	[-0.8, 1.0]	[-0.6, 0.8]
$\lambda_Z$	[-0.17, 0.17]	[-0.14, 0.14]	[-0.11, 0.11]

 $EWSB \times 1$  TeV scale

(Lee, Quigg, Thacker)

 $\ensuremath{\textcircled{O}}\xspace W_L^+ W_L^- \to W_L^+ W_L^-$  violates unitarity without EWSB

$$\label{eq:T} T(s,t) = \frac{A}{A} \left( \frac{p}{M_W} \right)^4 + \frac{B}{A} \left( \frac{p}{M_W} \right)^2 + C$$

 $\mathbf{A} = \mathbf{0}$  without the Higgs.



$$\textcircled{0} \text{ Including the Higgs: } \mathbf{a}_0 = -\frac{M_H^2}{16\pi v^2} \left[ 2 + \frac{M_H^2}{s - M_H^2} - \frac{M_H^2}{s} \log\left(1 + \frac{s}{M_H^2}\right) \right]$$

 $\textcircled{O} \text{ High energy limit: } \mathbf{a}_0 \stackrel{\mathbf{M}_{\mathbf{H}}^2 \ll s}{\longrightarrow} - \frac{\mathbf{M}_{\mathbf{H}}^2}{8\pi \mathbf{v}^2} \implies \mathbf{M}_{\mathbf{H}} < 870 \text{ GeV } (\mathbf{M}_{\mathbf{H}} < 710 \text{ GeV})$ 

 $\textcircled{O} \text{ No Higgs limit: } \mathbf{a}_0 \stackrel{\mathbf{M}_{H}^2 \gg s}{\longrightarrow} - \frac{\mathbf{s}}{32\pi \mathbf{v}^2} \implies \sqrt{\mathbf{s}_c} < 1.2 \text{ TeV}$ 

 $\rightleftharpoons$  In the limit  $p_g \rightarrow 0$ 

$$\mathcal{M}_1 = \overline{u}(p_q) \frac{\gamma_\alpha p_q'}{(p_q + p_g)^2} \mathcal{N} = \overline{u}(p_q) \frac{2p_{q\alpha}}{2p_q \cdot p_g} \mathcal{N} = \frac{p_{q\alpha}}{p_q \cdot p_g} \mathcal{M}$$

 $\Leftrightarrow$  The total amplitude for gluon emission is this limit is

$$egin{aligned} \mathcal{M}_{qar{q}g} &= \left(rac{p_{qlpha}}{p_q \cdot p_g} - rac{p_{ar{q}lpha}}{p_{ar{q}} \cdot p_g}
ight)\mathcal{M} \ &\\ \mathcal{M}|^2_{qar{q}g} &= 2rac{p_q \cdot p_{ar{q}}}{(p_q \cdot p_g)(p_{ar{q}} \cdot p_g)}|\mathcal{M}|^2. \end{aligned}$$

 $\Leftrightarrow$  After including the  $d\Phi_3$  we obtain (explain!)

$$\sigma^{q\bar{q}g} = \frac{2\alpha_s}{3\pi} \sigma_{q\bar{q}} \int d\cos\theta_{qg} \frac{dE_g}{E_g} \frac{4}{(1-\cos\theta_{qg})(1+\cos\theta_{qg})}.$$

the quark and antiquark are basically back to back in this limit.